



Unit 4

Electricity and Magnetism

Electricity Review

Two types of electric charge:

- Positive
- Negative

Opposites attract and likes repel

Electricity Review

- All matter is made up of protons, neutrons, and electrons.
 - Protons + charge
 - Neutrons 0 charge
 - Electrons - charge
- Electricity is caused by moving electric charges, specifically electrons.

Electron Freedom

Conductors: electrons are free to move

- Silver
- Gold
- Iron
- Steel
- The Human Body

Insulators: electrons are not free to move

- Glass
- Plastic
- Wood
- Rubber
- Fiberglass

Static Electricity

Electric charge imbalance on the surface of an object.

Common Occurrences:

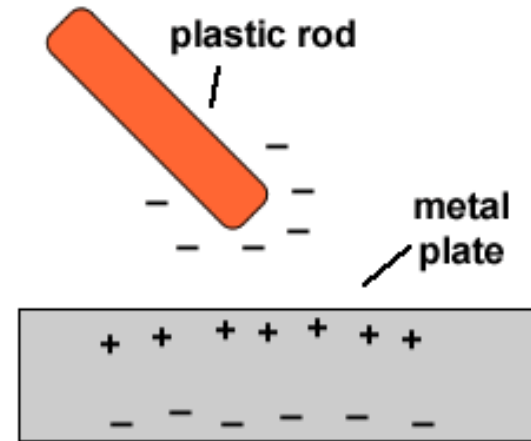
- Getting out of your car
- Walking along carpet



Polarization

A surface charge can be induced (caused or created) on an insulator

Hair comb picking up paper



Induction

Conductors can be given a charge by letting excess electrons move from one object to another

Grounding: A conducting material that is attached to Earth by another conducting material is *grounded*.

Induction

- Excess electrons can be provided by or removed by Earth
- Charge will flow from one conductor to another until electrical equilibrium is established or connection is broken.

[Conduction visuals](#)

Electric Forces

Unit of Charge: C (Coulomb)

Coulomb's Law $F_e = k \frac{q_1 q_2}{r^2}$

This equation is to be used for MAGNITUDE

- $k=9 \times 10^9 \text{ N m}^2/\text{C}^2$
- q : electric charge

Comparing F_E and F_g

$$F_e = k \frac{q_1 q_2}{r^2}$$

$$F_g = G \frac{m_1 m_2}{r^2}$$

k & G: constants (will be given)

q & m: How much stuff is there to exert a force
q can be negative but m can't

r & r: No difference between r's

Comparing F_E and F_g

$$F_e = k \frac{q_1 q_2}{r^2} \quad \text{and} \quad F_g = G \frac{m_1 m_2}{r^2}$$

Both forces have the same general form and are used the same way. Let us compare relative strengths of these two forces.

Which is holding matter together, F_E or F_g ?

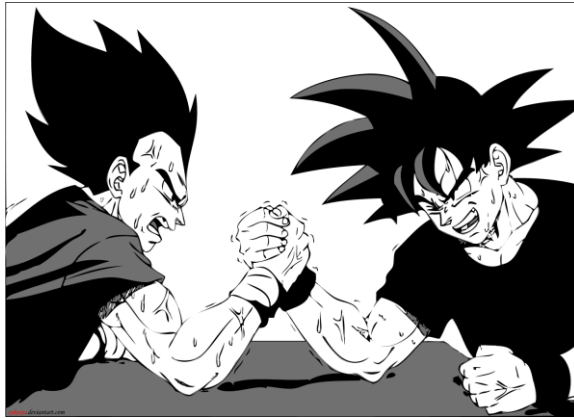
Comparing F_E and F_g

$$r = 5.3 \times 10^{-11}$$

$$G = 6.67 \times 10^{-11}$$

$$m_p = 1.67 \times 10^{-27}$$

$$m_e = 9.11 \times 10^{-31}$$



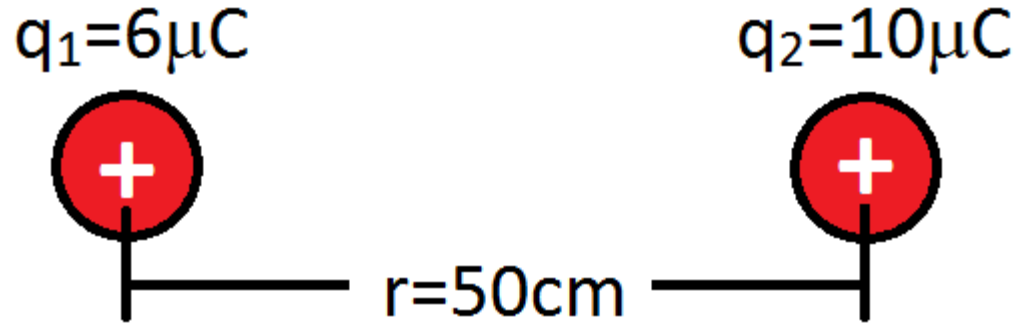
$$k = 9 \times 10^9$$

$$q_p = 1.6 \times 10^{-19}$$

$$q_e = -1.6 \times 10^{-19}$$

Example 1: 2 Charges, 1 Dimension

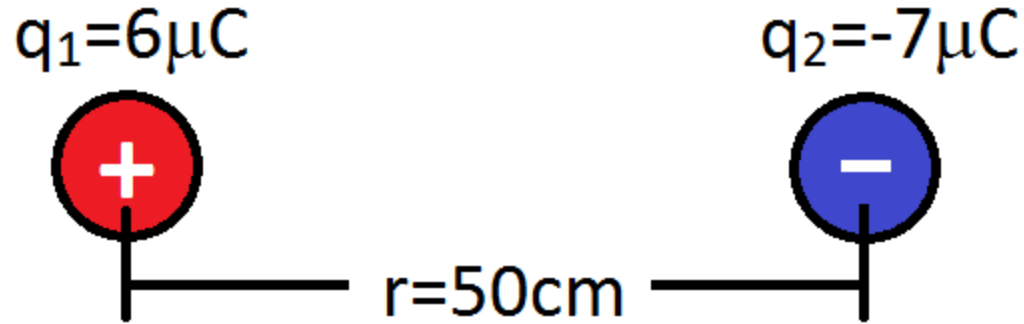
What is the force from q_1 on q_2 ?



$$F_e = 2.16\text{N in the positive x-direction or}$$
$$F_e = 2.16\mathbf{i} + 0\mathbf{j}$$

Example 2: 2 Charges, 1 Dimension

What is the force from q_1 on q_2 ?



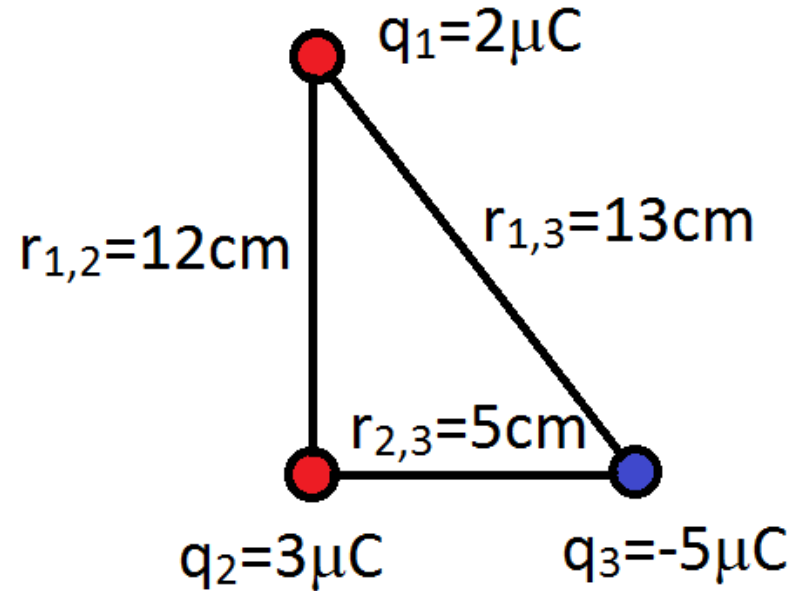
$F_e = 1.51\text{N}$ in the negative x-direction or
 $F_e = -1.51\mathbf{i} + 0\mathbf{j}$

How to Solve

1. Determine the magnitude and direction of $F_{1,3}$ and $F_{2,3}$.
2. Convert to $\mathbf{i}$ $\mathbf{j}$ notation.
3. Add the components of each force
4. Determine the magnitude and direction of net force, F_{net} .

Example 3: 3 Charges, 2 Dimensions

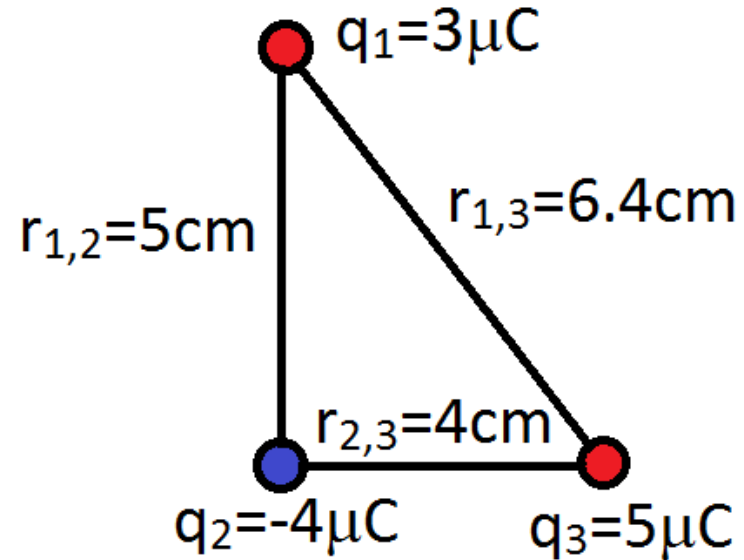
What is the force on q_3 from q_1 and q_2 ?



$$F_{\text{net}} = 56.27 \text{ N @ } 5.02^\circ \text{ above negative x-axis}$$

Example 4: 3 Charges, 2 Dimensions

What is the force on q_3
from q_1 and q_2 ?

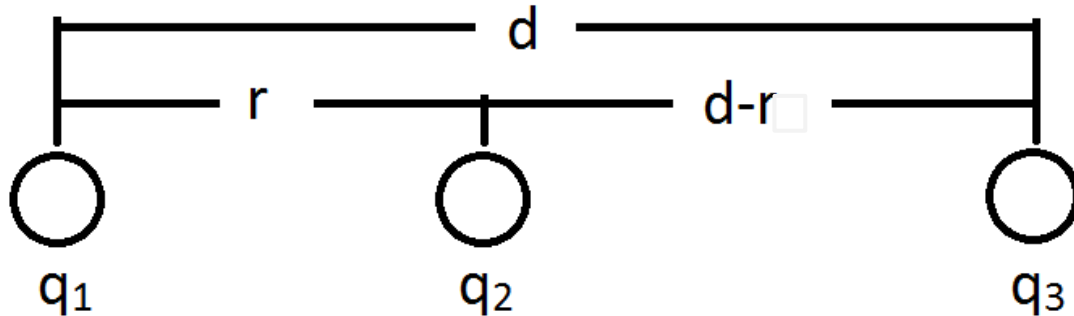


$$F_{\text{net}} = 95.45 \text{ N @ } 15.65^\circ \text{ below negative x-axis}$$

Example 5: Electrical Equilibrium

At what distance from q_1 will q_2 be at equilibrium?

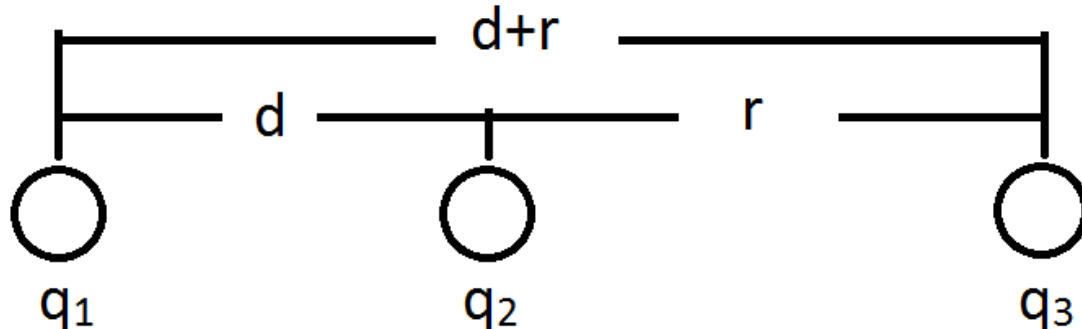
$$q_1 = 1\text{ }\mu\text{C}, q_2 = -2\text{ }\mu\text{C}, q_3 = 3\text{ }\mu\text{C}, d = 2\text{m}$$



Example 6: Electrical Equilibrium

At what distance from q_2 will q_3 be at equilibrium?

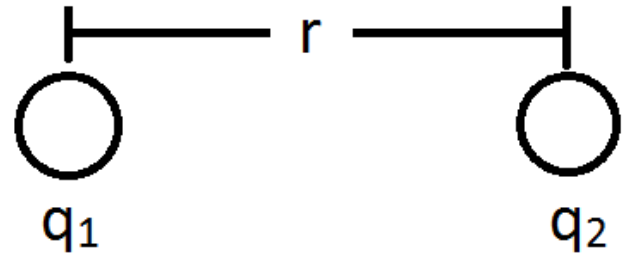
$$q_1 = 15 \mu\text{C}, q_2 = -6 \mu\text{C}, q_3 = 2 \mu\text{C}, d = 2\text{m}$$



Electric Fields

What is the force on q_2 from q_1 in each of the following examples?

- $q_1 = 2 \text{ C}$, $q_2 = 2 \text{ C}$, $r = 0.5 \text{ m}$
- $q_1 = 2 \text{ } \mu\text{C}$, $q_2 = 4 \text{ } \mu\text{C}$, $r = 0.5 \text{ m}$
- $q_1 = 2 \text{ } \mu\text{C}$, $q_2 = 6 \text{ } \mu\text{C}$, $r = 0.5 \text{ m}$



Electric Fields

- Notice that in every force equation there was something that was exactly the same in each example.
- $\frac{kq_1}{r^2}$ is the same in every equation!
- This is known as the electric field produced by q_1 .

Electric Fields

- A charged particle interacts with the electric field of another charged particle to produce electric forces
- $E_1 = \frac{kq_1}{r^2} \Rightarrow E_1q_2 = \frac{kq_1q_2}{r^2} = F_{1,2} \quad E_1q_2 = F_{1,2}$
- Electric fields are also vectors but just like forces, this equation is meant for magnitude.

Test Charge

- When working with Magnetic fields we often use a “test charge” to help with direction.
- Test charges are always positive and exist ONLY to show what direction a field will push/pull a positive charge.
- **Test charges** being **positive** is a **convention** so that all physicists agree on how electric fields behave

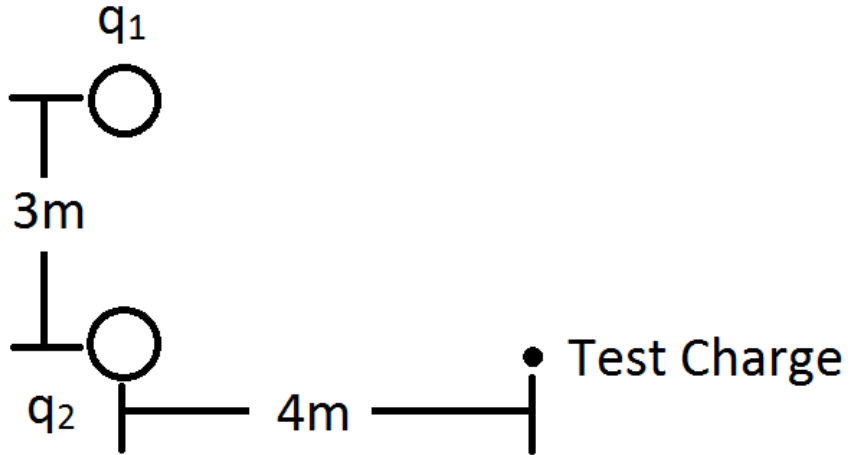
Example 7: Electric Field of 2 Charges

What is the magnitude and direction of the magnetic field a distance of 4m to the right of q_2 ?

($q_1=10 \text{ } \mu\text{C}$, $q_2=5 \text{ } \mu\text{C}$)

μ

μ



Electric Field Visualization

- The electric field of a charge = invisible hands that want to smack other electric charges around
- $E = k \frac{Q}{r^2}$ states that the invisible hands are weaker farther away from the charge.

Electric Field Vectors

- So what do physicists use to represent these invisible hands?
- Little arrows called VECTORS! :D

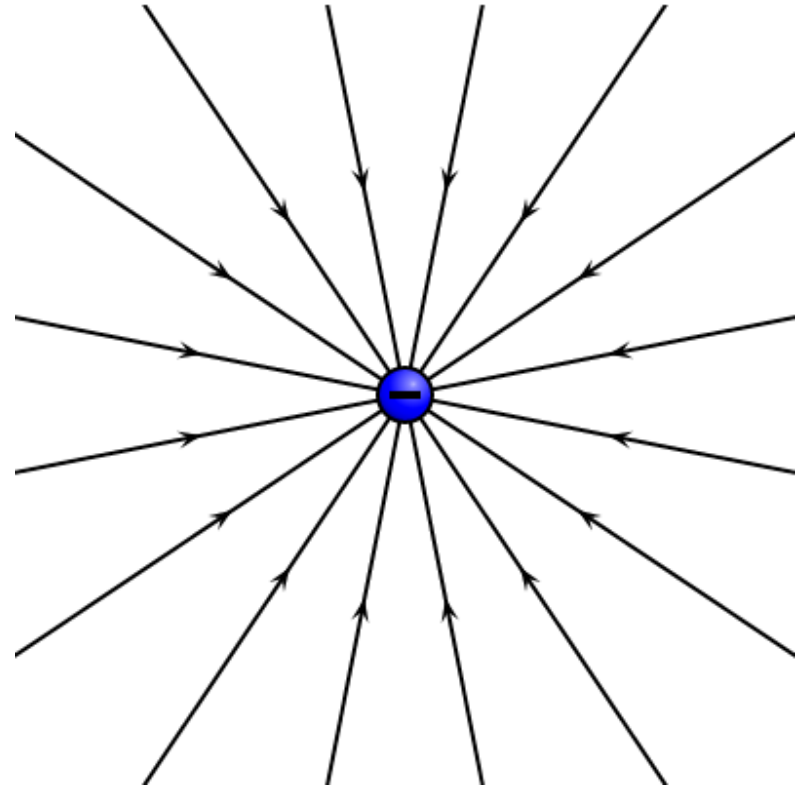
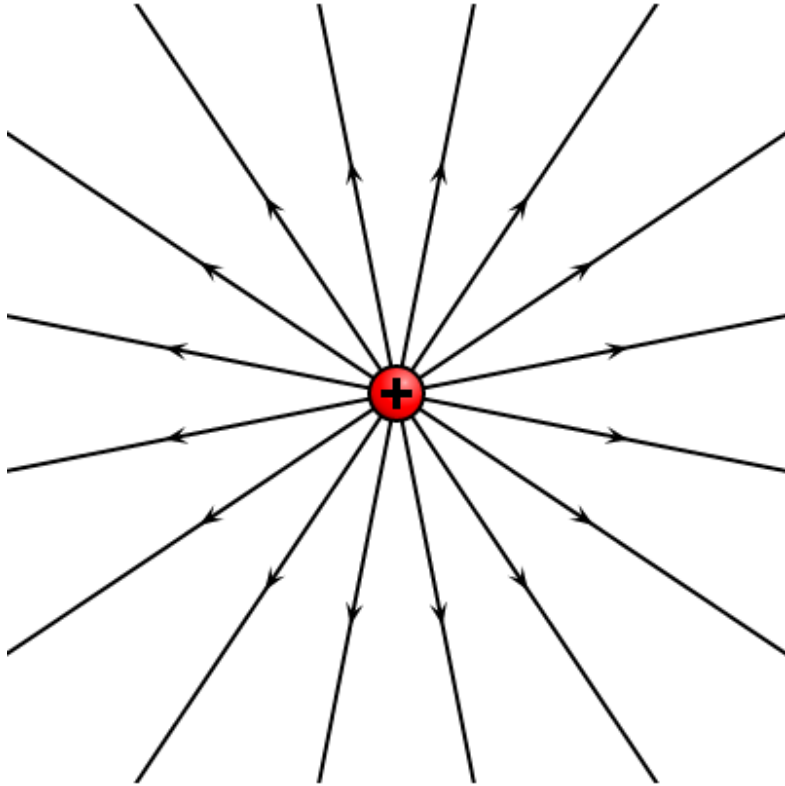
Electric Field Lines

- Instead of leaving an image of a bunch of little arrows, physicists connect the dots to form *Electric Field Lines*.

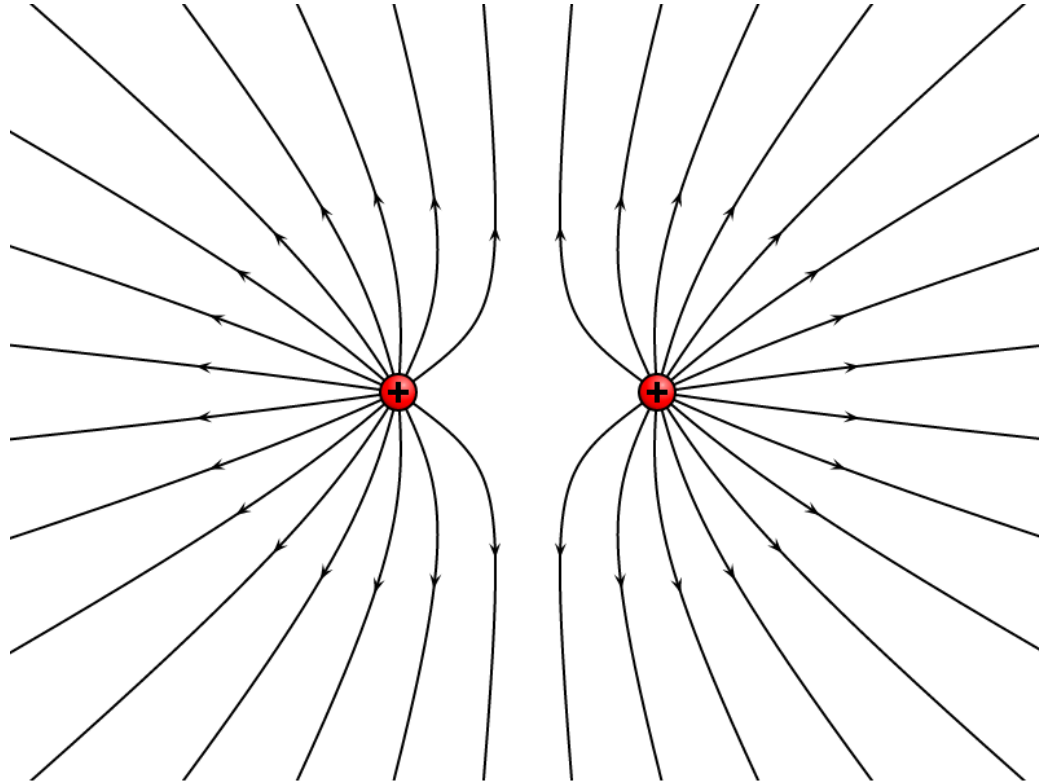


- Physicists remember farther away $\rightarrow$ = weaker

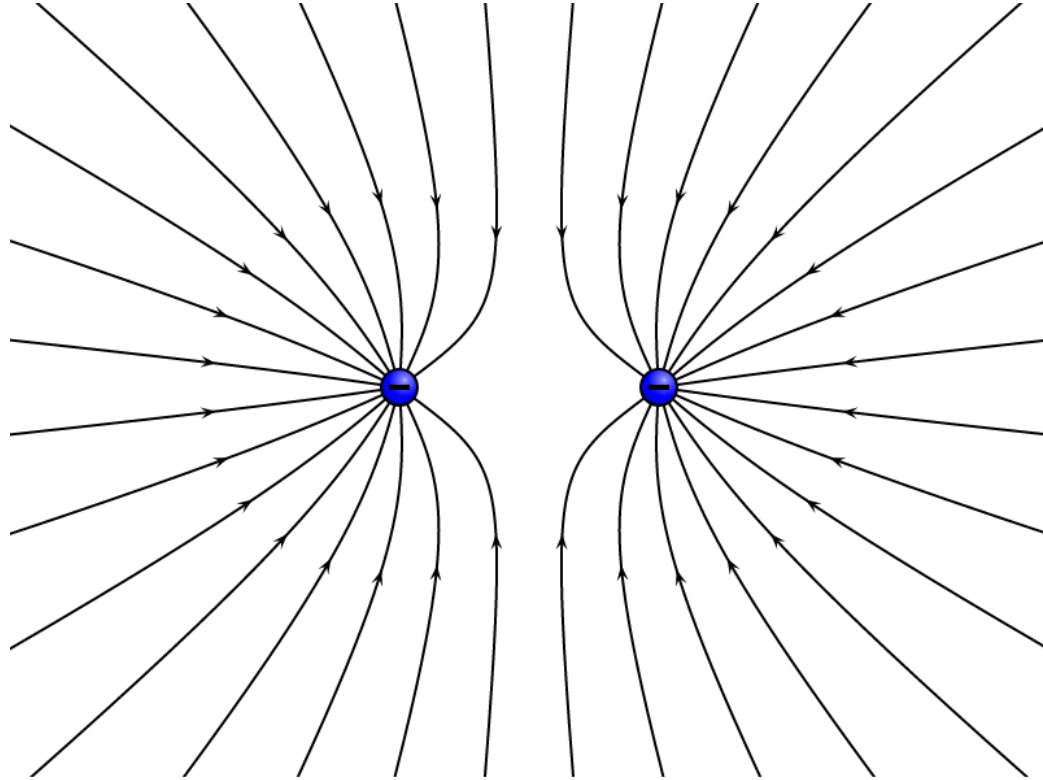
Positive and Negative Charges



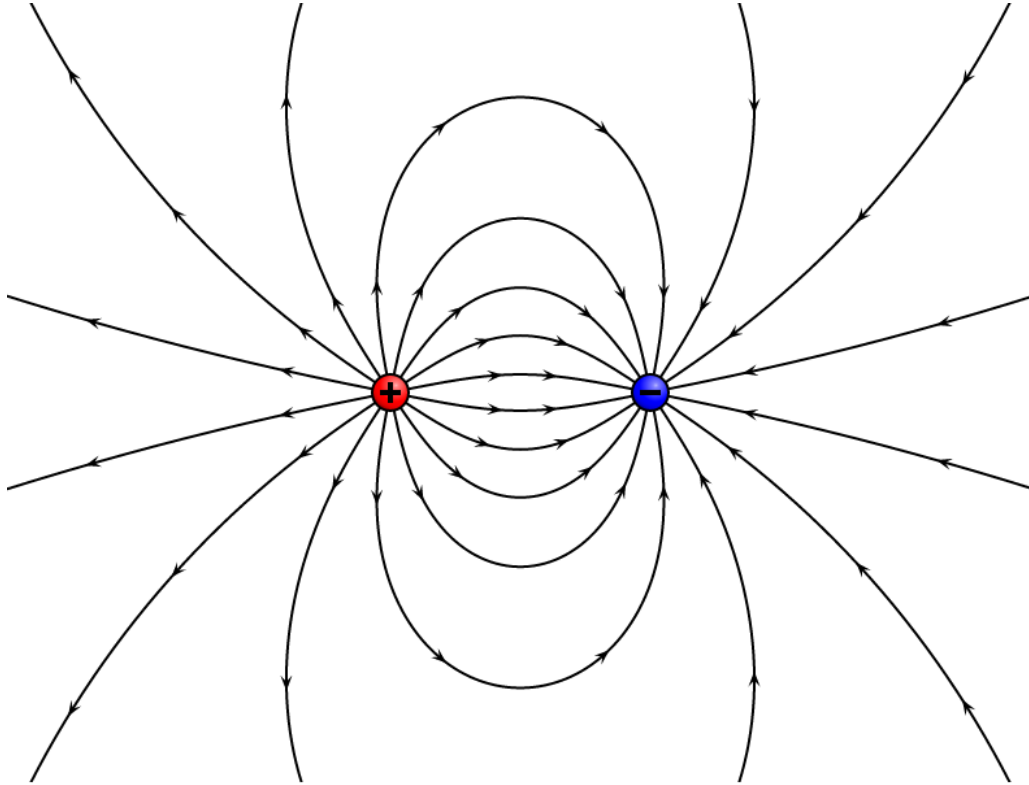
Positive-Positive



Negative-Negative



Positive-Negative



General Rules about Field Lines

- Field lines NEVER intersect!
- Field lines BEGIN on (point away from) positive charges
- Field lines END on (point toward) Negative charges

Force Fields? No. Forces AND Fields

- Non-contact forces can be described using the concept of a ***field***.
- A field is produced by charge Q is defined as

$$E = k \frac{Q}{r^2} \quad \text{or} \quad E = \frac{F}{q} \quad \text{where } q \text{ is the charge}$$

that would experience an electric force from Q.

Visualizing Electric Fields

- What direction does a test charge get “pushed/pulled” by a positive charge?
- What direction does a test charge get “pushed/pulled” by a negative charge?
- Draw arrows in the direction of the force that would be experienced if there were a charge there.

Calculating Electric Fields

What is the magnitude of the electric field at the center of this rectangular arrangement?

Figure 1:

